

# Heavy FLavor AVeraging group (HFLAV) - December 2017

Compilation of  $B^+$  Semi-leptonic and Radiative Branching Fractions ( $\times 10^{-6}$ ) - UL at 90% CL

**Preliminary      Updated results not included in PDG Live as of Dec. 31, 2017**

RPP#	Mode	PDG2017 Avg.	BABAR	Belle	LHCb	Our Avg.
428	$K^+\gamma$	$42.1 \pm 1.8$	$42.2 \pm 1.4 \pm 1.6$ [1]	$37.6 \pm 1.0 \pm 1.2$ [2]		$39.2 \pm 1.3$
429	$K_1^+(1270)\gamma$	$44^{+7}_{-6}$	$44^{+6.3}_{-4.4} \pm 5.8^\dagger$ [3]	$43 \pm 9 \pm 9$ [4]		$43.8^{+7.1}_{-6.3}$
430	$K^+\eta\gamma$	$7.9 \pm 0.9$	$7.7 \pm 1.0 \pm 0.4$ [5]	$8.4 \pm 1.5^{+1.2}_{-0.9}$ [6]		$7.9 \pm 0.9$
431	$K^+\eta'\gamma$	$2.9^{+1.0}_{-0.9}$	$1.9^{+1.5}_{-1.2} \pm 0.1$ [7]	$3.6 \pm 1.2 \pm 0.4$ [8]		$2.9^{+1.0}_{-0.9}$
432	$K^+\phi\gamma$	$2.7 \pm 0.4$	$3.5 \pm 0.6 \pm 0.4$ [9]	$2.48 \pm 0.30 \pm 0.24$ [10]		$2.71 \pm 0.34$
433	$K^+\pi^-\pi^+\gamma$	$25.8 \pm 1.5$	$25.9 \pm 0.7 \pm 1.0^\ddagger$ [3, 11]	$25.0 \pm 1.8 \pm 2.2^\dagger$ [4]		$25.8 \pm 1.1$
434	$K^0\pi^+\gamma$ §	$23.3 \pm 1.2$	$23.4 \pm 0.9^{+0.8}_{-0.7} \dagger$ [3]	$20^{+7}_{-6} \pm 2$ [12]		$23.3^{+1.2}_{-1.1}$
435	$K^+\rho^0\gamma$ §	$8.2 \pm 0.4 \pm 0.8^\dagger$	$8.2 \pm 0.4 \pm 0.8^\dagger$ [3]	$< 20$ [12]		$8.2 \pm 0.9$
	$(K\pi)^{*0}_0\pi^+\gamma$		$10.3^{+0.7+1.5}_{-0.8-2.0} \dagger$ [3]			$10.3^{+1.7}_{-2.2}$
436	$K^+\pi^-\pi^+\gamma$ (N.R.) §	$< 9.2$	$9.9 \pm 0.7^{+1.5}_{-1.9} \dagger$ [3]	$< 9.2$ [12]		$9.9^{+1.7}_{-2.0}$
440	$K_0^*(1430)\pi^+\gamma$	$1.32^{+0.09+0.24}_{-0.10-0.30} \dagger$	$1.32^{+0.09+0.24}_{-0.10-0.30} \dagger$ [3]			$1.32^{+0.26}_{-0.32}$
437	$K^0\pi^+\pi^0\gamma$	$46 \pm 5$	$45.6 \pm 4.2 \pm 3.1^\dagger$ [11]			$45.6 \pm 5.2$
438	$K_1^+(1400)\gamma$	$9.7^{+4.6+2.9}_{-2.9-2.4} \dagger$	$9.7^{+4.6+2.9}_{-2.9-2.4} \dagger$ [3]	$< 15$ [4]		$9.7^{+5.4}_{-3.8}$
439	$K^*(1410)\gamma$	$27.1^{+5.4+5.9}_{-4.8-3.7} \dagger$	$27.1^{+5.4+5.9}_{-4.8-3.7} \dagger$ [3]			$27.1^{+6.1}_{-5.1}$
441	$K_2^*(1430)^+\gamma$	$14 \pm 4$	$13.8^{+3.5+1.5}_{-3.2-1.0} \dagger$ [3, 13]			$13.8^{+3.8}_{-3.4}$
442	$K^{*+}(1680)\gamma$	$66.7^{+9.3+14.4}_{-7.8-11.4} \dagger$	$66.7^{+9.3+14.4}_{-7.8-11.4} \dagger$ [3]			$66.7^{+17.1}_{-13.8}$
443	$K_3^*(1780)^+\gamma$	$< 9900$		$< 39$ [6]		$< 39$
444	$K_3^*(2045)^+\gamma$	$< 39$		$< 39$ [6]		$< 39$
445	$\rho^+\gamma$	$0.98 \pm 0.25$	$1.20^{+0.42}_{-0.37} \pm 0.20$ [14]	$0.87^{+0.29+0.09}_{-0.27-0.11}$ [15]		$0.98^{+0.25}_{-0.24}$
495	$p\bar{\Lambda}\gamma$	$2.4^{+0.5}_{-0.4}$		$2.45^{+0.44}_{-0.38} \pm 0.22$ [16]		$2.45^{+0.49}_{-0.44}$
499	$p\Sigma^0\gamma$	$< 4.6$		$< 4.6$ [17]		$< 4.6$
534	$\pi^+\ell^+\ell^-$	$< 0.049$	$< 0.066$ [18]	$< 0.049$ [19]		$< 0.049$
535	$\pi^+e^+e^-$	$< 0.080$	$< 0.125$ [18]	$< 0.080$ [19]		$< 0.080$
536	$\pi^+\mu^+\mu^-$	$0.0179 \pm 0.0022 \pm 0.0005$	$< 0.055$ [18]	$< 0.069$ [19]	$0.0179 \pm 0.0022 \pm 0.0005$ [20]	$0.0180 \pm 0.0020$
537	$\pi^+\nu\bar{\nu}$	$< 98$	$< 100$ [21]	$< 98$ [22]		$< 98$
538	$K^+\ell^+\ell^-$	$0.451 \pm 0.023$	$0.48 \pm 0.09 \pm 0.02$ [23]	$0.53^{+0.05}_{-0.05} \pm 0.03$ [24]		$0.51 \pm 0.05$
539	$K^+e^+e^-$	$0.55 \pm 0.07$	$0.51^{+0.12}_{-0.11} \pm 0.02$ [23]	$0.57^{+0.09}_{-0.08} \pm 0.03$ [24]		$0.55 \pm 0.07$
540	$K^+\mu^+\mu^-$	$0.443 \pm 0.024$	$0.41^{+0.16}_{-0.15} \pm 0.02$ [23]	$0.53 \pm 0.08^{+0.07}_{-0.03}$ [24]	$0.429 \pm 0.007 \pm 0.021$ [25]	$0.435 \pm 0.021$
541	$K^+\tau^+\tau^-$	$< 2250$	$< 2250$ [26]			$< 2250$
542	$K^+\nu\bar{\nu}$	$< 16$	$< 16$ [27]	$< 16$ [28]		$< 16$
543	$\rho^+\nu\bar{\nu}$	$< 213$		$< 30$ [28]		$< 30$
	$\pi^+\nu\bar{\nu}$			$< 14$ [28]		$< 14$
544	$K^{*+}\ell^+\ell^-$	$1.01 \pm 0.11$	$1.40^{+0.40}_{-0.37} \pm 0.09$ [23]	$1.24^{+0.23}_{-0.21} \pm 0.13$ [24]	$0.924 \pm 0.093 \pm 0.067$ [29]	$1.009^{+0.101}_{-0.100}$
545	$K^{*+}e^+e^-$	$1.55^{+0.40}_{-0.31}$	$1.38^{+0.47}_{-0.42} \pm 0.08$ [23]	$1.73^{+0.50}_{-0.42} \pm 0.20$ [24]		$1.55^{+0.35}_{-0.32}$
546	$K^{*+}\mu^+\mu^-$	$0.96 \pm 0.10$	$1.46^{+0.79}_{-0.75} \pm 0.12$ [23]	$1.11^{+0.32}_{-0.27} \pm 0.10$ [24]	$0.924 \pm 0.093 \pm 0.067$ [29]	$0.958^{+0.107}_{-0.104}$
547	$K^{*+}\nu\bar{\nu}$	$< 40$	$< 64$ [27]	$< 40$ [22]		$< 40$
548	$K^{+}\pi^-\mu^+\mu^-$	$0.44 \pm 0.04$			$0.436^{+0.029}_{-0.027} \pm 0.028$ <sup>1</sup> [30]	$0.436^{+0.040}_{-0.039}$
549	$K^+\phi\mu^+\mu^-$	$0.079^{+0.021}_{-0.017}$			$0.082^{+0.019+0.029}_{-0.017-0.027}$ [30]	$0.082^{+0.035}_{-0.032}$

Channels with no RPP# are not reported by PDG.

Results for LHCb are relative BFs converted to absolute BFs.

CLEO upper limits that have been greatly superseded are not shown.

†  $M_{K\pi\pi} < 1.8$  GeV/c<sup>2</sup>.

‡  $1.0 < M_{K\pi\pi} < 2.0$  GeV/c<sup>2</sup>.

§  $M_{K\pi\pi} < 2.4$  GeV/c<sup>2</sup>.

¶ Average of BABAR results from [3] and [11].

◊ Average of BABAR results from [3] and [13].

<sup>1</sup> Differential BF in bins of  $m(\mu^+\mu^-)$  is also available.

# Heavy FLavor AVeraging group (HFLAV) - December 2017

Compilation of  $B^0$  Semi-leptonic and Radiative Branching Fractions ( $\times 10^{-6}$ ) - UL at 90% CL

**Preliminary**

**Updated results not included in PDG Live as of Dec. 31, 2017**

RPP #	Mode	PDG2017 Avg.	BABAR	Belle	LHCb	Our Avg.
367	$K^0\eta\gamma$	$7.6 \pm 1.8$	$7.1^{+2.1}_{-2.0} \pm 0.4$ [5]	$8.7^{+3.1+1.9}_{-2.7-1.6}$ [6]		$7.6^{+1.8}_{-1.7}$
368	$K^0\eta'\gamma$	$< 6.4$	$< 6.6$ [7]	$< 6.4$ [8]		$< 6.4$
369	$K^0\phi\gamma$	$2.7 \pm 0.7$	$< 2.7$ [9]	$2.74 \pm 0.60 \pm 0.32$ [10]		$2.74 \pm 0.68$
370	$K^+\pi^-\gamma$ <sup>§</sup>	$4.6 \pm 1.4$		$4.6^{+1.3+0.5}_{-1.2-0.7}$ [12]		$4.6 \pm 1.4$
371	$K^*\eta\gamma$	$43.3 \pm 1.5$	$44.7 \pm 1.0 \pm 1.6$ [1]	$39.6 \pm 0.7 \pm 1.4$ [2]		$41.7 \pm 1.2$
372	$K^*(1410)^0\gamma$	$< 130$		$< 130$ [12]		$< 130$
373	$K^+\pi^-\gamma$ (N.R.) <sup>†</sup>	$< 2.6$		$< 2.6$ [12]		$< 2.6$
374	$K^{*0}X(214), X(214) \rightarrow \mu^+\mu^-$	$< 0.0226$		$< 0.0226$ [31]		$< 0.0226$
375	$K^0\pi^+\pi^-\gamma$	$19.9 \pm 1.8$	$19.2 \pm 1.4 \pm 1.1$ <sup>‡</sup> [3, 11]	$24 \pm 4 \pm 3$ <sup>¶</sup> [4]		$19.7 \pm 1.7$
376	$K^+\pi^-\pi^0\gamma$	$41 \pm 4$	$40.7 \pm 2.2 \pm 3.1$ <sup>‡</sup> [11]			$40.7 \pm 3.8$
377	$K_1^0(1270)\gamma$	$< 58$		$< 58$ [4]		$< 58$
378	$K_1^0(1400)\gamma$	$< 12$		$< 12$ [4]		$< 12$
379	$K_2^*(1430)^0\gamma$	$12.4 \pm 2.4$	$12.2 \pm 2.5 \pm 1.0$ [13]	$13 \pm 5 \pm 1$ [12]		$12.4 \pm 2.4$
381	$K_3^*(1780)^0\gamma$	$< 83$		$< 83$ [6]		$< 83$
383	$\rho^0\gamma$	$0.86 \pm 0.15$	$0.97^{+0.24}_{-0.22} \pm 0.06$ [14]	$0.78^{+0.17+0.09}_{-0.16-0.10}$ [15]		$0.86^{+0.15}_{-0.14}$
384	$\rho^0X(214), X(214) \rightarrow \mu^+\mu^-$	$< 0.0173$		$< 0.0173$ [31]		$< 0.0173$
385	$\omega\gamma$	$0.44^{+0.18}_{-0.16}$	$0.50^{+0.27}_{-0.23} \pm 0.09$ [14]	$0.40^{+0.19}_{-0.17} \pm 0.13$ [15]		$0.44^{+0.18}_{-0.16}$
386	$\phi\gamma$	$< 0.1$	$< 0.85$ [32]	$< 0.1$ [33]		$< 0.1$
447	$p\bar{\Lambda}\pi^-\gamma$			$< 0.65$ [34]		$< 0.65$
503	$\pi^0\ell^+\ell^-$	$< 0.053$	$< 0.053$ [18]	$< 0.154$ [19]		$< 0.053$
504	$\pi^0e^+e^-$	$< 0.084$	$< 0.084$ [18]	$< 0.227$ [19]		$< 0.084$
505	$\pi^0\mu^+\mu^-$	$< 0.069$	$< 0.069$ [18]	$< 0.184$ [19]		$< 0.069$
506	$\eta\ell^+\ell^-$	$< 0.064$	$< 0.064$ [18]			$< 0.064$
507	$\eta e^+e^-$	$< 0.108$	$< 0.108$ [18]			$< 0.108$
508	$\eta\mu^+\mu^-$	$< 0.112$	$< 0.112$ [18]			$< 0.112$
509	$\pi^0\nu\bar{\nu}$	$< 69$		$< 9$ [28]		$< 9$
510	$K^0\ell^+\ell^-$	$0.31^{+0.08}_{-0.07}$	$0.21^{+0.15}_{-0.13} \pm 0.02$ [23]	$0.34^{+0.09}_{-0.08} \pm 0.02$ [24]		$0.31^{+0.08}_{-0.07}$
511	$K^0e^+e^-$	$0.16^{+0.10}_{-0.08}$	$0.08^{+0.12}_{-0.12} \pm 0.01$ [23]	$0.20^{+0.13}_{-0.10} \pm 0.01$ [24]		$0.16^{+0.10}_{-0.08}$
512	$K^0\mu^+\mu^-$	$0.339 \pm 0.034$	$0.49^{+0.29}_{-0.25} \pm 0.03$ [23]	$0.44^{+0.13}_{-0.10} \pm 0.03$ [24]	$0.327 \pm 0.034 \pm 0.017$ [29]	$0.343^{+0.036}_{-0.035}$
513	$K^0\nu\bar{\nu}$	$< 49$	$< 49$ [27]	$< 26$ [28]		$< 26$
514	$\rho^0\nu\bar{\nu}$	$< 208$		$< 40$ [28]		$< 40$
515	$K^*\ell^+\ell^-$	$0.99^{+0.12}_{-0.11}$	$1.03^{+0.22}_{-0.20} \pm 0.07$ [23]	$0.97^{+0.13}_{-0.12} \pm 0.07$ [24]		$0.99^{+0.13}_{-0.11}$
516	$K^0e^+e^-$	$1.03^{+0.19}_{-0.17}$	$0.86^{+0.26}_{-0.24} \pm 0.05$ [23]	$1.18^{+0.27}_{-0.22} \pm 0.09$ [24]		$1.03^{+0.19}_{-0.17}$
517	$K^0\mu^+\mu^-$	$1.03 \pm 0.06$	$1.35^{+0.40}_{-0.37} \pm 0.10$ [23]	$1.06^{+0.19}_{-0.14} \pm 0.07$ [24]	$1.036^{+0.018}_{-0.017} \pm 0.071$ <sup>1</sup> [35]	$1.049^{+0.067}_{-0.065}$
518	$K^{*0}X(214), X(214) \rightarrow \mu^+\mu^-$	$< 0.001$			$< 0.001$ [36]	$< 0.001$
519	$\pi^+\pi^-\mu^+\mu^-$	$0.021 \pm 0.005 \pm 0.001$			$0.0211 \pm 0.0051 \pm 0.0022$ <sup>°</sup> [37]	$0.0210 \pm 0.0060$
520	$K^0\nu\bar{\nu}$	$< 55$	$< 120$ [27]	$< 55$ [22]		$< 55$
523	$\phi\nu\bar{\nu}$	$< 127$		$< 127$ [22]		$< 127$
525	$\pi^0\mu^\mp$	$< 0.14$	$< 0.14$ [38]			$< 0.14$
526	$K^0e^\pm\mu^\mp$	$< 0.27$	$< 0.27$ [39]			$< 0.27$
527	$K^*e^+\mu^-$	$< 0.53$	$< 0.53$ [39]			$< 0.53$
528	$K^*e^-\mu^+$	$< 0.34$	$< 0.34$ [39]			$< 0.34$
529	$K^*e^\pm\mu^\mp$	$< 0.58$	$< 0.58$ [39]			$< 0.58$
532	$\Lambda_c^+\mu^-$	$< 1.4$	$< 1.4$ [40]			$< 1.4$
533	$\Lambda_c^+e^-$	$< 4$	$< 4$ [40]			$< 4$

Results for LHCb are relative BFs converted to absolute BFs.

CLEO upper limits that have been greatly superseded are not shown.

<sup>†</sup>  $1.25 \text{ GeV}/c^2 < M_{K\pi} < 1.6 \text{ GeV}/c^2$ .

<sup>‡</sup>  $M_{K\pi\pi} < 1.8 \text{ GeV}/c^2$ .

<sup>§</sup> Average of BABAR results from [3] and [11].

<sup>¶</sup>  $1.0 < M_{K\pi\pi} < 2.0 \text{ GeV}/c^2$ .

<sup>°</sup> This result takes into account the S-wave fraction in the  $K\pi$  system.

<sup>1</sup> Muon pairs do not originate from resonances and  $0.5 < m(\pi^+\pi^-) < 1.3 \text{ GeV}/c^2$ .

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Compilation of  $B$  Semi-leptonic and Radiative Branching Fractions ( $\times 10^{-6}$ ) - UL at 90% CL

Preliminary      Updated results not included in PDG Live as of Dec. 31, 2017

RPP#	Mode	PDG2017 Avg.	BABAR	Belle	CLEO	CDF	Our Avg.
67	$K\eta\gamma$	$8.5^{+1.8}_{-1.6}$		$8.5^{+1.3}_{-1.2} \pm 0.9$	[6]		$8.5^{+1.6}_{-1.5}$
68	$K_1(1400)\gamma$	$< 1.27$			$< 1.27$	[41]	$< 1.27$
69	$K_2^*(1430)\gamma$	$17^{+6}_{-5}$			$17 \pm 6 \pm 1$	[41]	$17 \pm 6$
71	$K_3^*(1780)\gamma$	$< 37$		$< 37^{\dagger}$	[6]		$< 37^{\dagger}$
78	$s\gamma^{\dagger}$	$349 \pm 19$	$341^{+28}_{-28} \ddagger$ [42–44]	$328^{+20}_{-20} \ddagger$ [45–47]	$329 \pm 44 \pm 29$	[48]	$332 \pm 15$
77	$s\gamma^{\circ}$		$308 \pm 22 \ddagger$ [42–44]	$305^{+16}_{-16} \ddagger$ [46, 47]			$306 \pm 12$
79	$d\gamma$	$9.2 \pm 3.0$	$9.2 \pm 2.0 \pm 2.3$ [49]				$9.2 \pm 3.0$
85	$\rho\gamma$	$1.39 \pm 0.25$	$1.73^{+0.34}_{-0.32} \pm 0.17$ [14]	$1.21^{+0.24}_{-0.22} \pm 0.12$ [15]			$1.39^{+0.22}_{-0.21}$
86	$\rho/\omega\gamma$	$1.30 \pm 0.23$	$1.63^{+0.30}_{-0.28} \pm 0.16$ [14]	$1.14 \pm 0.20^{+0.10}_{-0.12}$ [15]			$1.30^{+0.18}_{-0.19}$
121	$se^+e^- \ddagger$	$6.7 \pm 1.7$	$7.69^{+0.82+0.71}_{-0.77-0.60}$ [50]	$4.05 \pm 1.30^{+0.87}_{-0.83}$ [51]			$6.67 \pm 0.82$
120	$s\mu^+\mu^- \ddagger$	$4.3 \pm 1.0$	$4.41^{+1.31+0.63}_{-0.70-0.60}$ [50]	$4.13 \pm 1.05^{+0.85}_{-0.81}$ [51]			$4.27^{+0.98}_{-0.91}$
123	$s\ell^+\ell^- \ddagger$	$5.8 \pm 1.3$	$6.73^{+0.70-0.60}_{-0.64-0.56}$ [50]	$4.11 \pm 0.83^{+0.85}_{-0.81}$ [51]			$5.84 \pm 0.69$
124	$\pi\ell^+\ell^-$	$< 0.059$	$< 0.059$ [18]	$< 0.062$ [19]			$< 0.059$
125	$\pi e^+e^-$	$< 0.110$	$< 0.110$ [18]				$< 0.110$
126	$\pi\mu^+\mu^-$	$< 0.050$	$< 0.050$ [18]				$< 0.050$
127	$Ke^+e^-$	$0.44 \pm 0.06$	$0.39^{+0.09}_{-0.08} \pm 0.02$ [23]	$0.48^{+0.08}_{-0.07} \pm 0.03$ [24]			$0.44 \pm 0.06$
128	$K^*e^+e^-$	$1.19 \pm 0.20$	$0.99^{+0.23}_{-0.21} \pm 0.06$ [23]	$1.39^{+0.23}_{-0.20} \pm 0.12$ [24]			$1.19^{+0.17}_{-0.16}$
129	$K\mu^+\mu^-$	$0.44 \pm 0.04$	$0.41^{+0.13}_{-0.12} \pm 0.02$ [23]	$0.50 \pm 0.06 \pm 0.03$ [24]			$0.44 \pm 0.04$
130	$K^*\mu^+\mu^-$	$1.06 \pm 0.09$	$1.35^{+0.35}_{-0.33} \pm 0.10$ [23]	$1.10^{+0.16}_{-0.14} \pm 0.08$ [24]			$1.06 \pm 0.09$
131	$K\ell^+\ell^-$	$0.48 \pm 0.04$	$0.47 \pm 0.06 \pm 0.02$ [53]	$0.48^{+0.05}_{-0.04} \pm 0.03$ [24]			$0.48 \pm 0.04$
132	$K^*\ell^+\ell^-$	$1.05 \pm 0.10$	$1.02^{+0.14}_{-0.13} \pm 0.05$ [53]	$1.07^{+0.11}_{-0.10} \pm 0.09$ [24]			$1.05 \pm 0.10$
133	$K\nu\bar{\nu}$	$< 17$	$< 17$ [27]	$< 16$ [28]			$< 16$
134	$K^*\nu\bar{\nu}$	$< 76$	$< 76$ [27]	$< 27$ [28]			$< 27$
	$\pi\nu\bar{\nu}$			$< 9$ [28]			$< 9$
	$\rho\nu\bar{\nu}$			$< 30$ [28]			$< 30$
136	$\pi e^+\mu^\mp$	$< 0.092$	$< 0.092$ [38]				$< 0.092$
137	$\rho e^+\mu^\mp$	$< 3.2$			$< 3.2$	[54]	$< 3.2$
138	$Ke^\pm\mu^\mp$	$< 0.038$	$< 0.038$ [39]				$< 0.038$
139	$K^*e^\pm\mu^\mp$	$< 0.51$	$< 0.51$ [39]				$< 0.51$

Channels with no RPP# are not reported by PDG.

Results for CDF are relative BFs converted to absolute BFs.

CLEO upper limits that have been greatly superseded are not shown.

<sup>†</sup> Results extrapolated to  $E_\gamma > 1.6$  GeV, using the method of Ref. [55].

<sup>‡</sup> Belle:  $m(\ell^+\ell^-) > 0.2$  GeV/ $c^2$ , BABAR:  $m^2(\ell^+\ell^-) > 0.1$  GeV $^2/c^4$ .

<sup>§</sup> The value quoted is  $\mathcal{B}(B \rightarrow K_3^*\gamma) \times \mathcal{B}(K_3^* \rightarrow K\eta)$ . PDG gives the BF assuming  $\mathcal{B}(K_3^* \rightarrow K\eta) = 11^{+5}_{-4}\%$ .

<sup>¶</sup> Average of several results, obtained with different methods.

<sup>◦</sup> Only results originally measured in the interval  $E_\gamma > 1.9$  GeV (also taken into account in the previous line).

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Compilation of  $B^+$  and  $B^0$  Leptonic Branching Fractions ( $\times 10^{-6}$ ) - UL at 90% CL

**Preliminary      Updated results not included in PDG Live as of Dec. 31, 2017**

RPP#	Mode	PDG2017 Avg.	BABAR	Belle	CDF	LHCb	CMS	ATLAS	Our Avg.
31	$e^+\nu$	< 0.98	< 1.9 [56]	< 0.98 <sup>†</sup> [57]					< 0.98 <sup>†</sup>
32	$\mu^+\nu$	< 1.0	< 1.0 [56]	< 1.7 <sup>†</sup> [57]					< 1.0
33	$\tau^+\nu$	$109 \pm 24$	$183^{+53}_{-49} \pm 24$ <sup>‡</sup> [58]	$125 \pm 28 \pm 27$ <sup>‡</sup> [59]					$144 \pm 31$
34	$\ell^+\nu_e\gamma$	< 3.5	< 15.6 [60]	< 3.5 [61]					< 3.5
35	$e^+\nu_e\gamma$	< 6.1	< 17 [60]	< 6.1 [61]					< 6.1
36	$\mu^+\nu_\mu\gamma$	< 3.4	< 24 [60]	< 3.4 [61]					< 3.4
495	$\gamma\gamma$	< 0.32	< 0.32 [62]	< 0.62 [63]					< 0.32
458	$e^+e^-$	< 0.083	< 0.113 [64]	< 0.19 [65]	< 0.083 [66]				< 0.083
497	$e^+\nu_e\gamma$	< 0.12	< 0.12 [67]						< 0.12
498	$\mu^+\nu_\mu$	$0.00018^{+3.1}_{-3.1}$	< 0.052 [64]	< 0.16 [65]	< 0.0038 [68]	< 0.00034 <sup>¶</sup> [69]	< 0.00110 <sup>¶</sup> [70]	$-0.25^{+0.20}_{-0.20} \mathfrak{¶}$ [71]	$0.00039^{+0.00016}_{-0.00014}$
499	$\mu^+\mu^-\gamma$	< 0.16	< 0.16 [67]						< 0.16
500	$\mu^+\mu^-\mu^+\mu^-$	< 0.0053			< 0.0053 <sup>¶</sup> [72]				< 0.0053 <sup>¶</sup>
501	$SP, S \rightarrow \mu^+\mu^-, P \rightarrow \mu^+\mu^-$	< 0.0051			< 0.0051 <sup>¶</sup> [72]				< 0.0051 <sup>¶</sup>
502	$\tau^+\tau^-$	< 4100	< 4100 [73]			< 1600 [74]			< 1600
524	$e^\pm\mu^\mp$	< 0.0028	< 0.092 [64]	< 0.17 [65]	< 0.064 [66]	< 0.001 <sup>¶</sup> [75]			< 0.001
530	$e^\pm\tau^\mp$	< 28	< 28 [76]						< 28
532	$\mu^\pm\tau^\mp$	< 22	< 22 [76]						< 22
521	$\nu\bar{\nu}$	< 24	< 24 [77]	< 130 [78]					< 24
522	$\nu\bar{\nu}\gamma$	< 17	< 17 [77]						< 17

Results for CDF, LHCb, CMS and ATLAS are relative BFs converted to absolute BFs.

<sup>†</sup> More recent results exist, with hadronic tagging [79], that do not improve the limits (< 3.5 and < 2.7) for  $e^+\nu$  and  $\mu^+\nu$ , respectively).

<sup>‡</sup> The authors make the average with their previous results, derived from statistically independent samples [80, 81].

<sup>§</sup> This is the combined result obtained by the LHCb and CMS collaborations [82].

<sup>¶</sup> UL at 95% CL.

Heavy FLavor AVeraging group (HFLAV) - December 2017  
 Compilation of  $B$  Relative Semi-leptonic and Radiative Branching Fractions  
 Preliminary      Updated results not included in PDG Live as of Dec. 31, 2017

RPP#	Mode	PDG2017 AVG.	Belle	BABAR	LHCb	Our Avg.
548/298	$10^4 \times \mathcal{B}(K^+ \pi^+ \pi^- \mu^+ \mu^-) / \mathcal{B}(\psi(2S) K^+)$	$6.95^{+0.46}_{-0.46} \pm 0.34$			$6.95^{+0.46}_{-0.46} \pm 0.34$ [30]	$6.95^{+0.57}_{-0.55}$
549/274	$10^4 \times \mathcal{B}(K^+ \phi \mu^+ \mu^-) / \mathcal{B}(\psi(2S) K^+)$	$1.58^{+0.36}_{-0.36} \pm 0.19$			$1.58^{+0.36}_{-0.32} \pm 0.19$ [30]	$1.58^{+0.41}_{-0.33}$
536/540	$\mathcal{B}(\pi^+ \mu^+ \mu^-) / \mathcal{B}(K^+ \mu^+ \mu^-)^\dagger$	$0.053 \pm 0.014 \pm 0.01$			$0.038 \pm 0.009 \pm 0.001$ [20]	$0.038 \pm 0.009$
	$\mathcal{B}(K^+ \mu^+ \mu^-) / \mathcal{B}(K^+ e^+ e^-)^\ddagger$					$1.00^{+0.32}_{-0.25} \pm 0.07$ [53]
	$\mathcal{B}(K^* \mu^+ \mu^-) / \mathcal{B}(K^* e^+ e^-)^\S$		$0.83 \pm 0.17 \pm 0.08$ [24]			$0.83 \pm 0.19$
	$\mathcal{B}(K^* \mu^+ \mu^-) / \mathcal{B}(K^* e^+ e^-)^\P$			$1.013^{+0.34}_{-0.26} \pm 0.010$ [53]		$1.013^{+0.34}_{-0.26}$
	$\mathcal{B}(K^{*0} \mu^+ \mu^-) / \mathcal{B}(K^{*0} e^+ e^-)^\diamond$				$0.66^{+0.11}_{-0.07} \pm 0.03$ [83]	$0.66^{+0.12}_{-0.08}$
	$\mathcal{B}(K^{*0} \mu^+ \mu^-) / \mathcal{B}(K^{*0} e^+ e^-)^\circlearrowleft$				$0.69^{+0.11}_{-0.07} \pm 0.05$ [83]	$0.69^{+0.12}_{-0.09}$
	$\mathcal{B}(B^0 \rightarrow K^{*0} \gamma) / \mathcal{B}(B_s^0 \rightarrow \phi \gamma)$	$1.10 \pm 0.16 \pm 0.09 \pm 0.18$ [2]			$1.23 \pm 0.06 \pm 0.11$ [84]	$1.21 \pm 0.11$

Channels with no RPP# are not reported by PDG.

$\dagger$  For  $0.1 < m^2(\ell^+ \ell^-) < 6.0 \text{ GeV}^2/c^4$ .

$\ddagger$  For  $1.0 < m^2(\ell^+ \ell^-) < 6.0 \text{ GeV}^2/c^4$ .

$\S$  For the full  $m^2(\ell^+ \ell^-)$  range.

$\P$  For  $0.10 < m^2(\ell^+ \ell^-) < 8.12 \text{ GeV}^2/c^4$  and  $m^2(\ell^+ \ell^-) > 10.11 \text{ GeV}^2/c^4$ .

$\diamond$  For  $0.045 < m^2(\ell^+ \ell^-) < 1.1 \text{ GeV}^2/c^4$ .

$\circlearrowleft$  For  $1.1 < m^2(\ell^+ \ell^-) < 6.0 \text{ GeV}^2/c^4$ .

## Heavy FLavor AVeraging group (HFLAV) - December 2017

Compilation of Branching Fractions of  $B^+/B^0$  to  $\bar{q}$  gluon decays ( $\times 10^{-6}$ ) - UL at 90% CL

Preliminary      Updated results not included in PDG Live as of Dec. 31, 2017

RPP#	Mode	PDG2017 Avg.	BABAR	Belle	CLEO	Our Avg.
81	$\eta X$	$260^{+50}_{-80}$		$261 \pm 30^{+44}_{-74} \S [85]$	$< 440$ [86]	$261^{+53}_{-79}$
81	$\eta' X$	$420 \pm 90$	$390 \pm 80 \pm 90 \dagger [87]$		$460 \pm 110 \pm 60 \dagger [88]$	$423 \pm 86$
83	$K^+ X$	$< 187$	$< 187 \ddagger$ [89]			$< 187 \ddagger$
84	$K^0 X$	$190^{+70}_{-70}$	$195^{+51}_{-45} \pm 50 \ddagger [89]$			$195^{+71}_{-67}$
95	$\pi^+ X$	$370 \pm 80$	$372^{+50}_{-47} \pm 59 \P [89]$			$372^{+77}_{-75}$

$\dagger$   $2.0 < p^*(\eta') < 2.7$  GeV/ $c$ .

$\ddagger$   $m_X < 1.69$  GeV/ $c^2$ .

$\S$   $0.4 < m_X < 2.6$  GeV/ $c^2$ .

$\P$   $m_X < 1.71$  GeV/ $c^2$ .

Heavy FLavor AVeraging group (HFLAV) - December 2017  
Isospin Asymmetry

Preliminary      Updated results not included in PDG Live as of Dec. 31, 2017

Parameter	PDG2017 Avg.	<i>BABAR</i>	<i>Belle</i>	<i>LHCb</i>	Our Avg.
$\Delta_{0^-}(X_s\gamma)$	$-0.01 \pm 0.06$	$-0.01^{+0.06}_{-0.06} \dagger$ [42, 90]			$-0.01 \pm 0.06$
$\Delta_{0^+}(K^*\gamma)$	$0.052 \pm 0.026$	$0.066 \pm 0.021 \pm 0.022$ [1]	$0.062 \pm 0.015 \pm 0.006 \pm 0.012$ [2]		$0.063 \pm 0.017$
$\Delta_{\rho\gamma}$	$-0.46 \pm 0.17$	$-0.43^{+0.25}_{-0.22} \pm 0.10$ [14]	$-0.48^{+0.21+0.08}_{-0.19-0.09}$ [15]		$-0.46^{+0.17}_{-0.16}$
$\Delta_{0^-}(K\ell\ell)^\dagger$	$-0.13 \pm 0.06$	$-0.58^{+0.29}_{-0.37} \pm 0.02$ [53]	$-0.31^{+0.17}_{-0.14} \pm 0.08$ [24]	$-0.10^{+0.08}_{-0.09} \pm 0.02 \ddagger$ [29]	$-0.17 \pm 0.08$
$\Delta_{0^-}(K^*\ell\ell)^\dagger$	$-0.45 \pm 0.17$	$-0.64^{+0.15}_{-0.14} \pm 0.03$ [53]	$0.30^{+0.12}_{-0.11} \pm 0.08$ [24]	$0.00^{+0.12}_{-0.10} \pm 0.02 \ddagger$ [29]	$-0.06 \pm 0.07$

In some of the  $B$ -factory results it is assumed that  $\mathcal{B}(\Upsilon(4S) \rightarrow B^+ B^-) = \mathcal{B}(\Upsilon(4S) \rightarrow B^0 \bar{B}^0)$ , and in others a measured value of the ratio of branching fractions is used. See original papers for details. The averages quoted above are computed naively and should be treated with caution.

<sup>†</sup> Results given for the bin  $1 < m^2(\ell^+\ell^-) < 6$  GeV $^2/c^4$ , see references for the other bins.

<sup>‡</sup> Average of two independent measurements from *BABAR* [42, 90].

<sup>§</sup> Only muons are used.

Heavy FLavor AVeraging group (HFLAV) - December 2017

Compilation of  $B^+$  Semi-leptonic LFV & LNV Branching Fractions ( $\times 10^{-6}$ ) - UL at 90% CL

**Preliminary      Updated results not included in PDG Live as of Dec. 31, 2017**

RPP#	Mode	PDG2017 Avg.	BABAR	BELLE	LHCb	Our Avg.
552	$\pi^+ e^\pm \mu^\mp$	< 0.17	< 0.17 [38]			< 0.17
553	$\pi^+ e^+ \tau^-$	< 74	< 74 [91]			< 74
554	$\pi^+ e^- \tau^+$	< 20	< 20 [91]			< 20
555	$\pi^+ e^\pm \tau^\mp$	< 75	< 75 [91]			< 75
556	$\pi^+ \mu^+ \tau^-$	< 62	< 62 [91]			< 62
557	$\pi^+ \mu^- \tau^+$	< 45	< 45 [91]			< 45
558	$\pi^+ \mu^\pm \tau^\mp$	< 72	< 72 [91]			< 72
559	$K^+ e^+ \mu^-$	< 0.091	< 0.091 [39]			< 0.091
560	$K^+ e^- \mu^+$	< 0.13	< 0.13 [39]			< 0.13
561	$K^+ e^\pm \mu^\mp$	< 0.091	< 0.091 [39]			< 0.091
562	$K^+ e^+ \tau^-$	< 43	< 43 [91]			< 43
563	$K^+ e^- \tau^+$	< 15	< 15 [91]			< 15
564	$K^+ e^\pm \tau^\mp$	< 30	< 30 [91]			< 30
565	$K^+ \mu^+ \tau^-$	< 45	< 45 [91]			< 45
566	$K^+ \mu^- \tau^+$	< 28	< 28 [91]			< 28
567	$K^+ \mu^\pm \tau^\mp$	< 48	< 48 [91]			< 48
568	$K^{*-} e^+ \mu^-$	< 1.3	< 1.3 [39]			< 1.3
569	$K^{*-} e^- \mu^+$	< 0.99	< 0.99 [39]			< 0.99
570	$K^{*-} e^\pm \mu^\mp$	< 1.4	< 1.4 [39]			< 1.4
571	$\pi^- e^+ e^+$	< 0.023	< 0.023 [92]			< 0.023
572	$\pi^- \mu^+ \mu^+$	< 0.013	< 0.107 [92]		< 0.004 † [93]	< 0.004 †
573	$\pi^- e^+ \mu^+$	< 0.15	< 0.15 [94]			< 0.15
574	$\rho^- e^+ e^+$	< 0.17	< 0.17 [94]			< 0.17
575	$\rho^- \mu^+ \mu^+$	< 0.42	< 0.42 [94]			< 0.42
576	$\rho^- e^+ \mu^+$	< 0.47	< 0.47 [94]			< 0.47
577	$K^- e^+ e^+$	< 0.03	< 0.03 [92]			< 0.03
578	$K^- \mu^+ \mu^+$	< 0.041	< 0.067 [92]		< 0.041 [95]	< 0.041
579	$K^- e^+ \mu^+$	< 0.16	< 0.16 [94]			< 0.16
580	$K^{*-} e^+ e^+$	< 0.40	< 0.40 [94]			< 0.40
581	$K^{*-} \mu^+ \mu^+$	< 0.59	< 0.59 [94]			< 0.59
582	$K^{*-} e^+ \mu^+$	< 0.30	< 0.30 [94]			< 0.30
583	$D^- e^+ e^+$	< 2.6	< 2.6 [94]	< 2.6 [96]		< 2.6
584	$D^- e^+ \mu^+$	< 1.8	< 2.1 [94]	< 1.8 [96]		< 1.8
585	$D^- \mu^+ \mu^+$	< 0.69	< 1.7 [94]	< 1.1 [96]	< 0.69 [97]	< 0.69
586	$D_s^- \mu^+ \mu^+$	< 0.58			< 0.58 [97]	< 0.58
587	$\bar{D}^0 \pi^- \mu^+ \mu^+$	< 1.5			< 1.5 [97]	< 1.5
589	$\Lambda^0 \mu^+$	< 0.06	< 0.06 [40]			< 0.06
590	$\Lambda^0 e^+$	< 0.032	< 0.032 [40]			< 0.032
591	$\bar{\Lambda}^0 \mu^+$	< 0.06	< 0.06 [40]			< 0.06
592	$\bar{\Lambda}^0 e^+$	< 0.08	< 0.08 [40]			< 0.08

Results for LHCb are relative BFs converted to absolute BFs.

CLEO upper limits that have been greatly superseded are not shown.

† UL at 95% CL.

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